

Infinite Geometric Series

Determine if each geometric series converges or diverges.

1) $a_1 = -3, r = 4$

2) $a_1 = 4, r = -\frac{3}{4}$

3) $a_1 = 5.5, r = 0.5$

4) $a_1 = -1, r = 3$

5) $81 + 27 + 9 + 3\ldots,$

6) $7.1 + 17.75 + 44.375 + 110.9375\ldots,$

7) $-3 + \frac{12}{5} - \frac{48}{25} + \frac{192}{125}\ldots,$

8) $\frac{128}{3125} - \frac{64}{625} + \frac{32}{125} - \frac{16}{25}\ldots,$

9) $\sum_{k=1}^{\infty} -4^{k-1}$

10) $\sum_{k=1}^{\infty} \frac{16}{9} \left(\frac{3}{2}\right)^{k-1}$

11) $\sum_{i=1}^{\infty} 4.2 \cdot 0.2^{i-1}$

12) $\sum_{k=1}^{\infty} \frac{7}{6} \left(-\frac{1}{4}\right)^{k-1}$

Evaluate each infinite geometric series described.

13) $a_1 = 3, r = -\frac{1}{5}$

14) $a_1 = 1, r = -4$

15) $a_1 = 1, r = -3$

16) $a_1 = 1, r = \frac{1}{2}$

$$17) \ 1 + 0.5 + 0.25 + 0.125\dots,$$

$$18) \ 3 - \frac{9}{4} + \frac{27}{16} - \frac{81}{64}\dots,$$

$$19) \ 81 - 27 + 9 - 3\dots,$$

$$20) \ 1 - 0.6 + 0.36 - 0.216\dots,$$

$$21) \ \sum_{k=1}^{\infty} 5 \cdot \left(-\frac{1}{5}\right)^{k-1}$$

$$22) \ \sum_{n=1}^{\infty} -6 \cdot \left(-\frac{1}{2}\right)^{n-1}$$

$$23) \ \sum_{i=1}^{\infty} \left(\frac{1}{3}\right)^{i-1}$$

$$24) \ \sum_{k=1}^{\infty} 4^{k-1}$$

Determine the common ratio of the infinite geometric series.

$$25) \ a_1 = 1, \ S = 1.25$$

$$26) \ a_1 = 96, \ S = 64$$

$$27) \ a_1 = -4, \ S = -\frac{16}{5}$$

$$28) \ a_1 = 1, \ S = 2.5$$

Infinite Geometric Series

Determine if each geometric series converges or diverges.

1) $a_1 = -3, r = 4$

Diverges

2) $a_1 = 4, r = -\frac{3}{4}$

Converges

3) $a_1 = 5.5, r = 0.5$

Converges

4) $a_1 = -1, r = 3$

Diverges

5) $81 + 27 + 9 + 3\dots,$

Converges

6) $7.1 + 17.75 + 44.375 + 110.9375\dots,$

Diverges

7) $-3 + \frac{12}{5} - \frac{48}{25} + \frac{192}{125}\dots,$

Converges

8) $\frac{128}{3125} - \frac{64}{625} + \frac{32}{125} - \frac{16}{25}\dots,$

Diverges

9) $\sum_{k=1}^{\infty} -4^{k-1}$

Diverges

10) $\sum_{k=1}^{\infty} \frac{16}{9} \left(\frac{3}{2}\right)^{k-1}$

Diverges

11) $\sum_{i=1}^{\infty} 4.2 \cdot 0.2^{i-1}$

Converges

12) $\sum_{k=1}^{\infty} \frac{7}{6} \left(-\frac{1}{4}\right)^{k-1}$

Converges

Evaluate each infinite geometric series described.

13) $a_1 = 3, r = -\frac{1}{5}$

$\frac{5}{2}$

15) $a_1 = 1, r = -3$

No sum

14) $a_1 = 1, r = -4$

No sum

16) $a_1 = 1, r = \frac{1}{2}$

2

$$17) 1 + 0.5 + 0.25 + 0.125\dots,$$

2

$$18) 3 - \frac{9}{4} + \frac{27}{16} - \frac{81}{64}\dots,$$

$$\frac{12}{7}$$

$$19) 81 - 27 + 9 - 3\dots,$$

$$\frac{243}{4}$$

$$20) 1 - 0.6 + 0.36 - 0.216\dots,$$

$$0.625$$

$$21) \sum_{k=1}^{\infty} 5 \cdot \left(-\frac{1}{5}\right)^{k-1}$$

$$\frac{25}{6}$$

$$22) \sum_{n=1}^{\infty} -6 \cdot \left(-\frac{1}{2}\right)^{n-1}$$

$$-4$$

$$23) \sum_{i=1}^{\infty} \left(\frac{1}{3}\right)^{i-1}$$

$$\frac{3}{2}$$

$$24) \sum_{k=1}^{\infty} 4^{k-1}$$

No sum

Determine the common ratio of the infinite geometric series.

$$25) a_1 = 1, S = 1.25$$

$$0.2$$

$$26) a_1 = 96, S = 64$$

$$-\frac{1}{2}$$

$$27) a_1 = -4, S = -\frac{16}{5}$$

$$-\frac{1}{4}$$

$$28) a_1 = 1, S = 2.5$$

$$0.6$$