Name_____
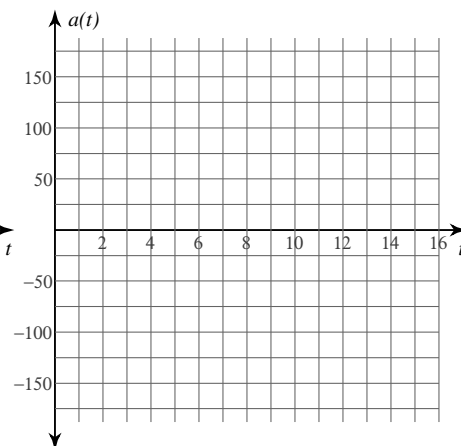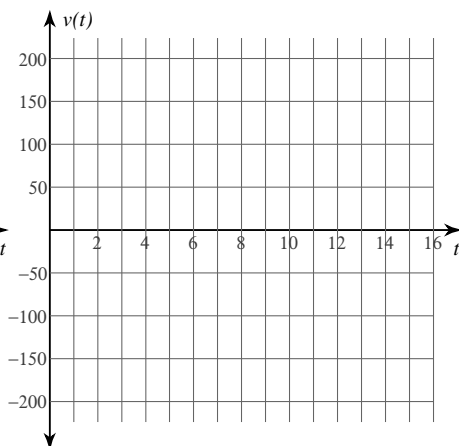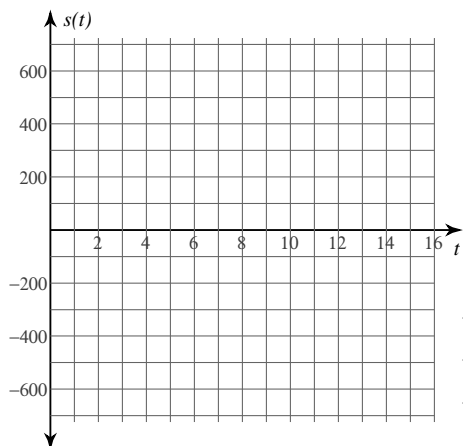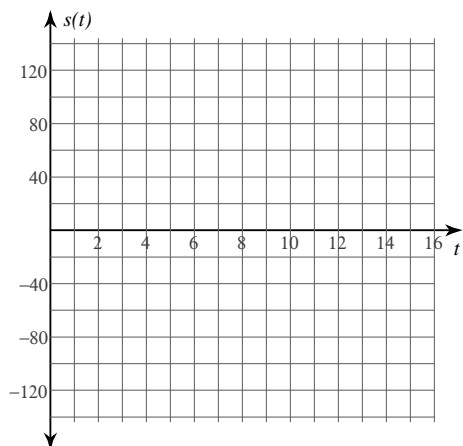
# Motion Along a Line

Date_____ Period_____

**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the velocity function $v(t)$ and the acceleration function $a(t)$. You may use the blank graphs to sketch $s(t)$, $v(t)$, and $a(t)$.**
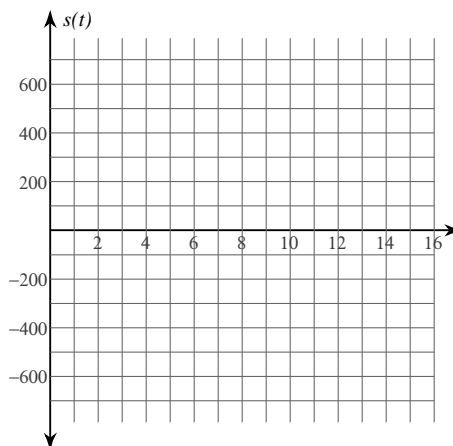
1) $s(t) = t^3 - t^2 - 56t$



**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the displacement of the particle and the distance traveled by the particle over the given interval. You may use the blank graph to sketch $s(t)$.**
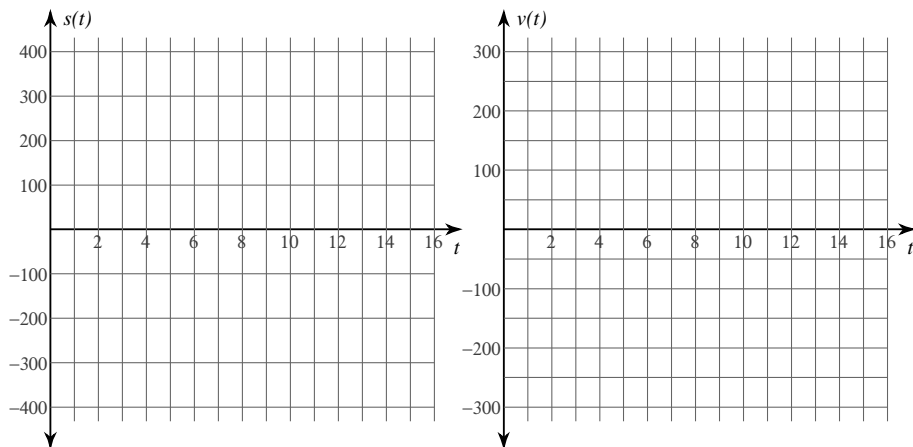
2) $s(t) = -t^2 + 6t + 27;\ 0 \leq t \leq 4$
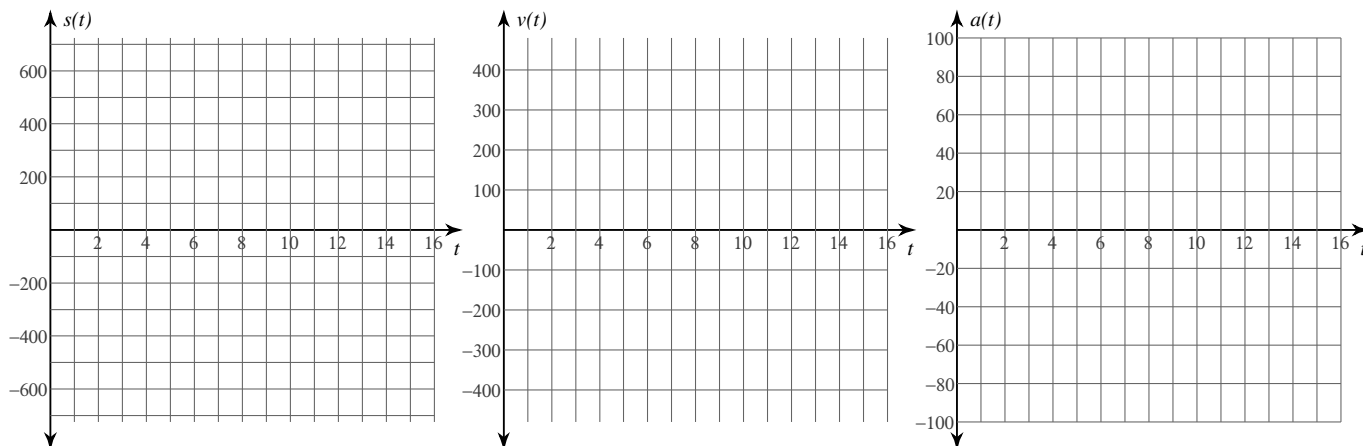


3) $s(t) = -t^3 + 11t^2;\ 3 \leq t \leq 8$

**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the maximum speed and times $t$ when this speed occurs over the given interval. You may use the blank graphs to sketch $s(t)$ and $v(t)$.**

4) $s(t) = -t^3 + 18t^2 - 81t; \ \ 2 \leq t \leq 7$

**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the velocity function $v(t)$, the acceleration function $a(t)$, the times $t$ when the particle changes directions, the intervals of time when the particle is moving left and moving right, the times $t$ when the acceleration is 0, and the intervals of time when the particle is slowing down and speeding up. You may use the blank graphs to sketch $s(t)$, $v(t)$, and $a(t)$.**
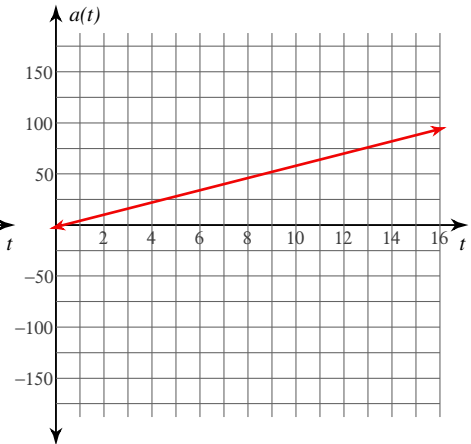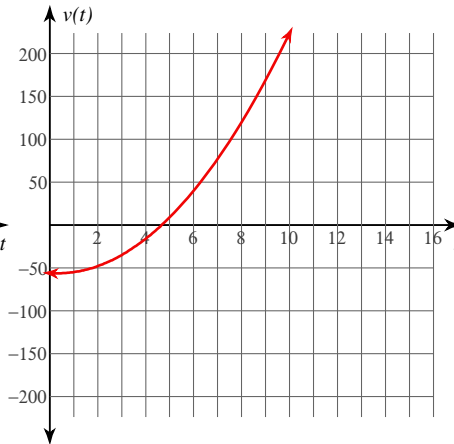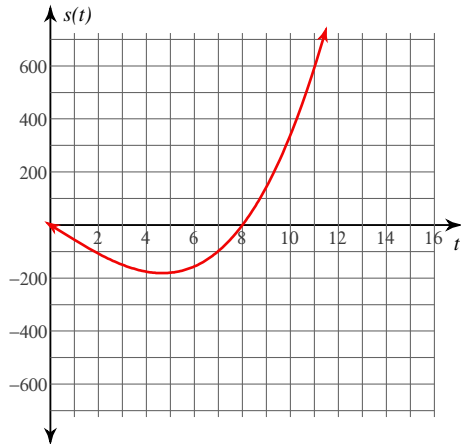
5) $s(t) = t^3 - 23t^2 + 120t$

Name_____

# Motion Along a Line

Date_____ Period_____

**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the velocity function $v(t)$ and the acceleration function $a(t)$. You may use the blank graphs to sketch $s(t)$, $v(t)$, and $a(t)$.**
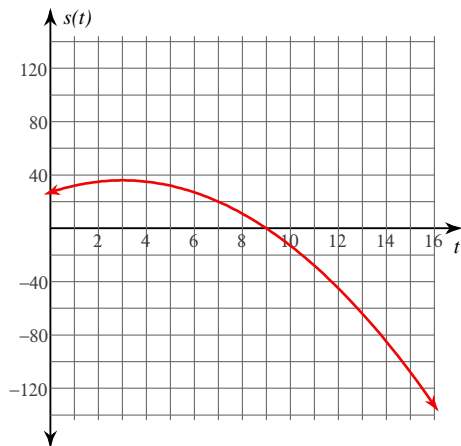
1) $s(t) = t^3 - t^2 - 56t$
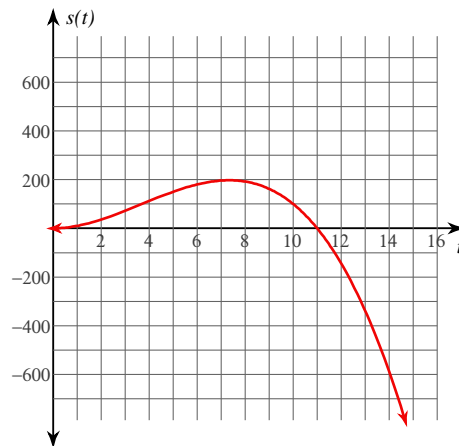


$v(t) = 3t^2 - 2t - 56, \ a(t) = 6t - 2$

**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the displacement of the particle and the distance traveled by the particle over the given interval. You may use the blank graph to sketch $s(t)$.**

2) $s(t) = -t^2 + 6t + 27; \ 0 \leq t \leq 4$


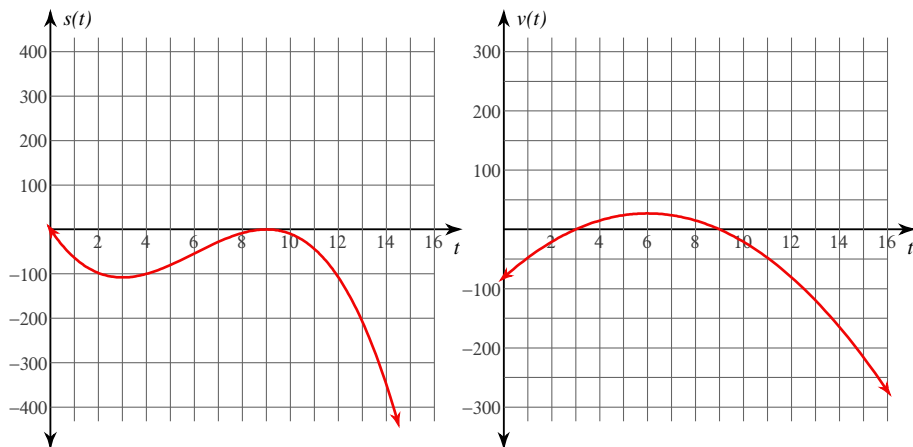
Displacement: 8
Distance traveled: 10

3) $s(t) = -t^3 + 11t^2; \ 3 \leq t \leq 8$



Displacement: 120
Distance traveled: $\dfrac{3520}{27} \approx 130.37$

**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the maximum speed and times $t$ when this speed occurs over the given interval. You may use the blank graphs to sketch $s(t)$ and $v(t)$.**

4) $s(t) = -t^3 + 18t^2 - 81t; \quad 2 \leq t \leq 7$



Maximum speed: 27 at $t = \{6\}$

**A particle moves along a horizontal line. Its position function is $s(t)$ for $t \geq 0$. For each problem, find the velocity function $v(t)$, the acceleration function $a(t)$, the times $t$ when the particle changes directions, the intervals of time when the particle is moving left and moving right, the times $t$ when the acceleration is 0, and the intervals of time when the particle is slowing down and speeding up. You may use the blank graphs to sketch $s(t)$, $v(t)$, and $a(t)$.**

5) $s(t) = t^3 - 23t^2 + 120t$
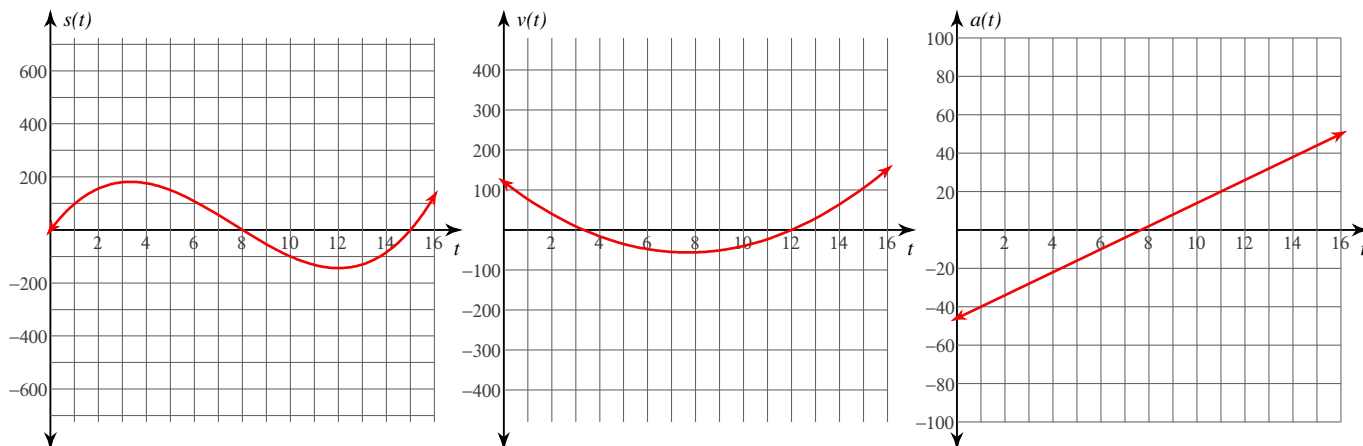


$v(t) = 3t^2 - 46t + 120, \ a(t) = 6t - 46$

Changes direction at: $t = \left\{\dfrac{10}{3}, 12\right\}$, Moving left: $\dfrac{10}{3} < t < 12$, Moving right: $0 \leq t < \dfrac{10}{3}, t > 12$

Acceleration zero at: $t = \left\{\dfrac{23}{3}\right\}$, Slowing down: $0 \leq t < \dfrac{10}{3}, \dfrac{23}{3} < t < 12$, Speeding up: $\dfrac{10}{3} < t < \dfrac{23}{3}, t > 12$